

# Development of 2D Local Searching Algorithms for Surface Determination of X-ray Computed Tomography Measurement

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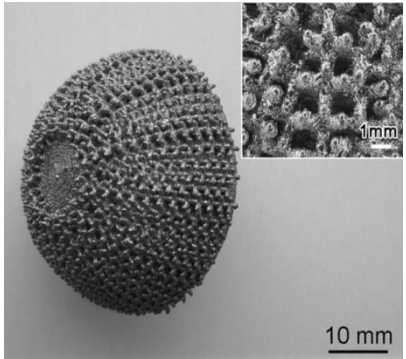
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# Outline

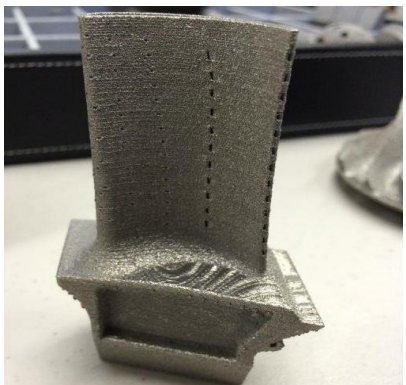
1. Introduction
2. Simulation procedure
3. 2D Local Searching Algorithm
4. Initial results
5. Summary & future work

# 1. Introduction

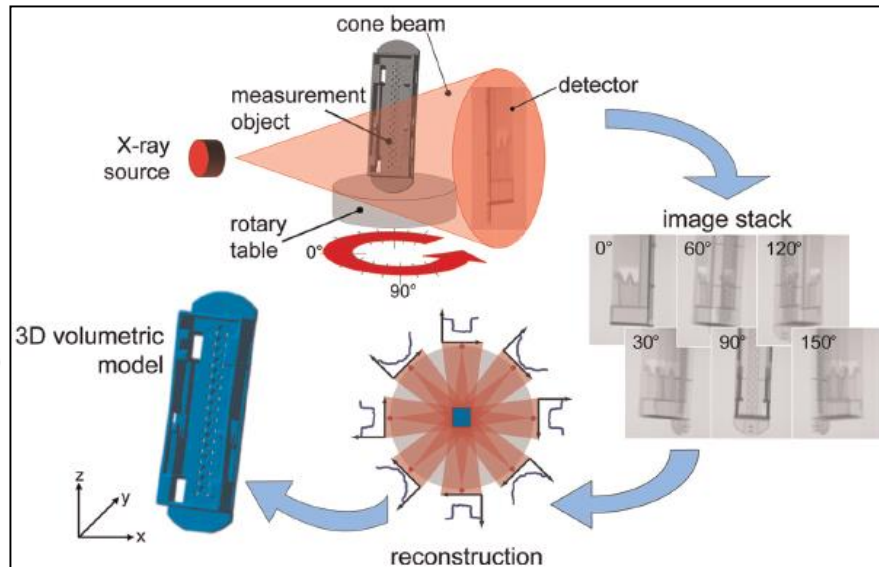
- XCT for geometrical measurement



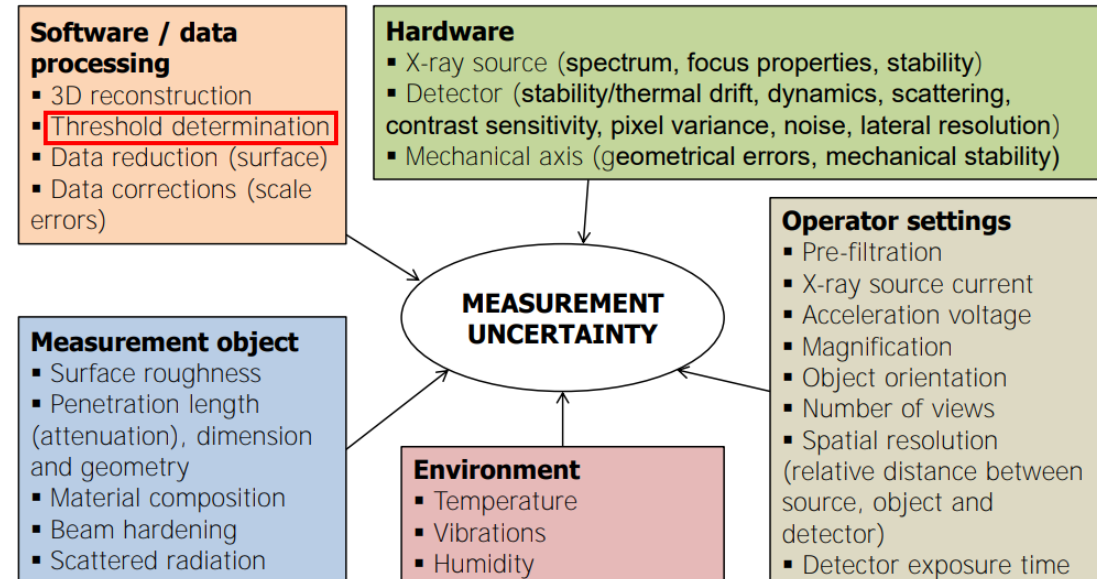
Acetabular cup with a porous structure (SLM)



Aircraft turbine blade (EBM)



Working Principle of XCT  
[A. Weckenmann et al. 2012]

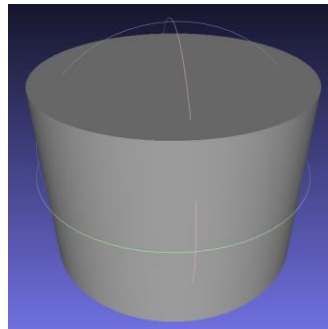


XCT measurement uncertainty [Pavel et al. 2013]

Ref 1: Weckenmann A. et al. 2012 Computed tomography in quality control: chances and challenges *Proc ImechE Part B*

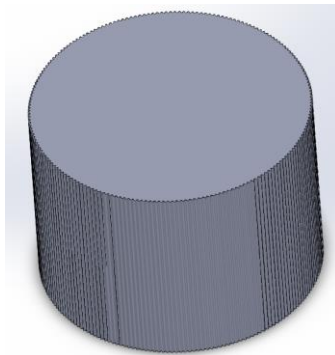
Ref 2: Pavel M. et al. 2013 Coordinate Metrology by Traceable Computed Tomography

# 2. Simulation procedure

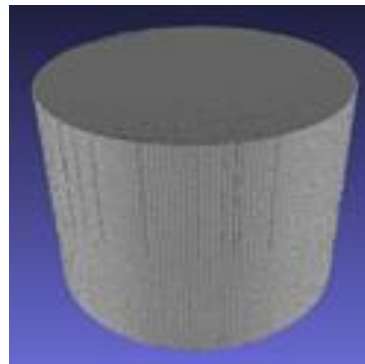


Smooth cylinder (radius: 7 mm)

CAD design



Convert to mesh

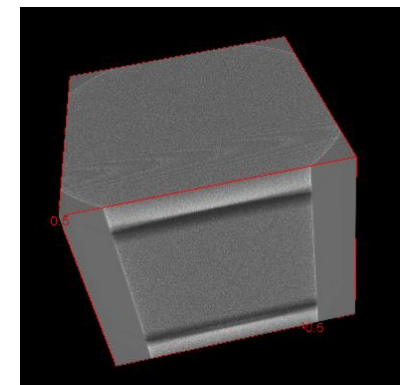


XCT scanning simulation



aRTist

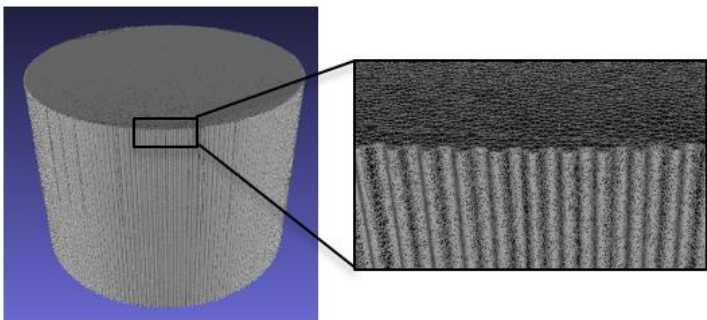
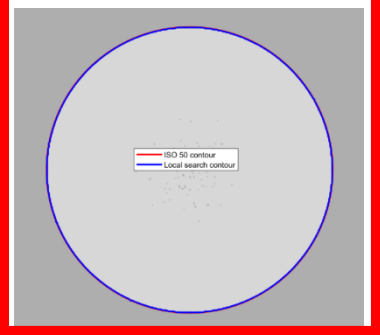
Volumetric reconstruction



Cross-sectioning



Surface determination



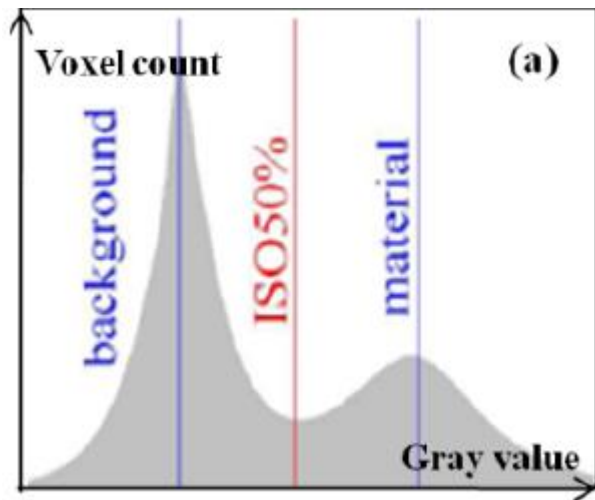
Rough cylinder (radius: 7 mm)

$$\begin{cases} x = (7 + 0.05 \sin(200t)) \cdot \sin(t) \\ y = (7 + 0.05 \sin(200t)) \cdot \cos(t) \end{cases} \quad t \in [0, 2\pi]$$

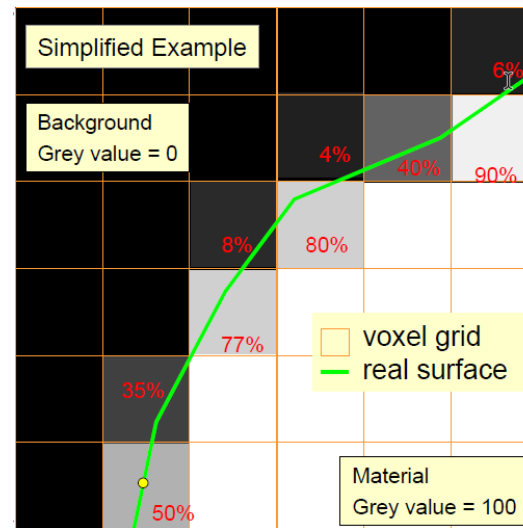
Amplitude: 50  $\mu$ m, Period  $\pi/100$

# 3. 2D Local Searching Algorithms

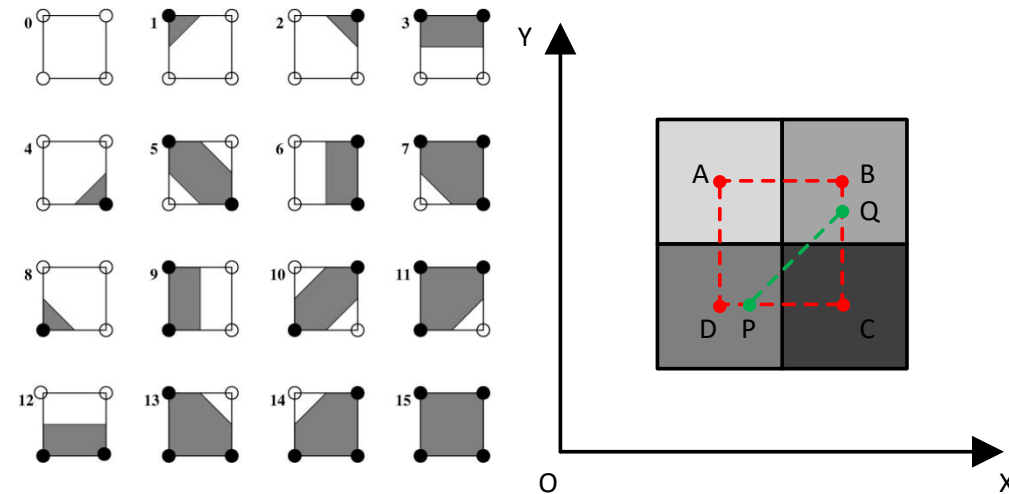
- Initial contour: ISO 50 + Marching square



ISO 50 threshold [Tan et al. 2011]



Partial volume effect [Reinhart 2011 ]



Marching square [Mantz 2008 ]

$$\frac{Q_y - B_y}{D_y - B_y} = \frac{ISO50 - I(B)}{I(D) - I(B)} \Rightarrow Q_y = B_y + \frac{ISO50 - I(B)}{I(D) - I(B)}$$

Ref 1: Tan Y, et al. Material Dependent Thresholding for Dimensional X-ray Computed Tomography, 2011.

Ref 2: Reinhart C Industrial CT & Precision, Volume Graphics GmbH, 2011.

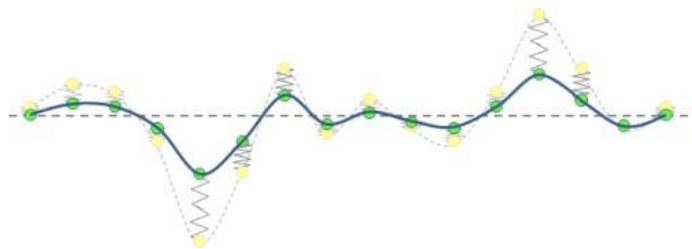
Ref 3: Mantz et al. Utilizing Minkowski functionals for image analysis: a marching square algorithm, 2008

# 3. 2D Local Searching Algorithms

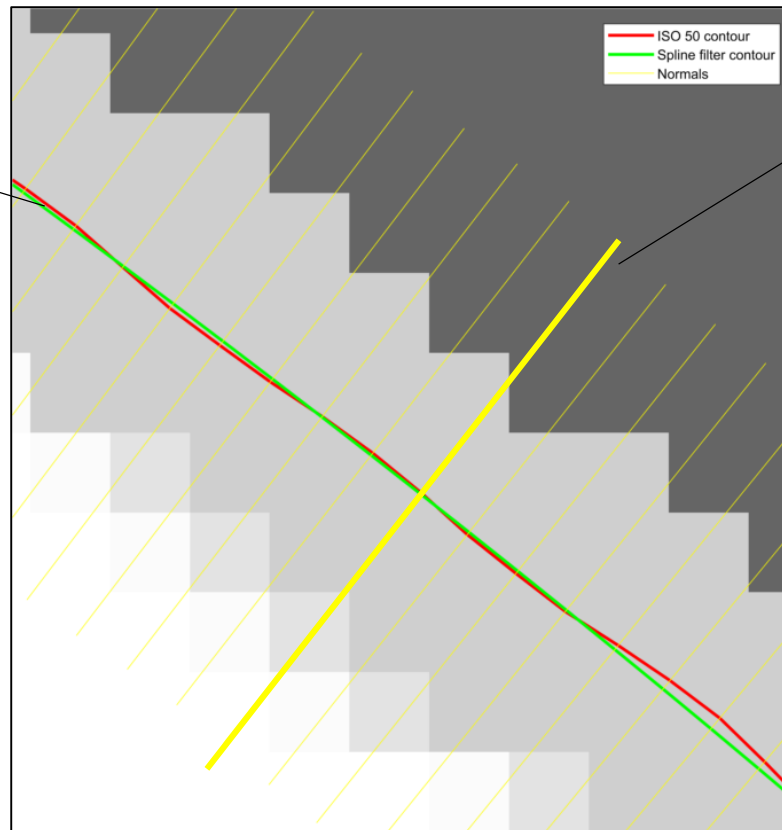
- Searching maximum gradient along the normal vectors of the initial contour

Spline filter is used to smooth the initial contour and thus generates more stable contour normal.

**Optimisation problem:**  
Find the spline minimizing the **square** of the **residual errors** under the conditioning of minimizing the **bending energy** of the spline.

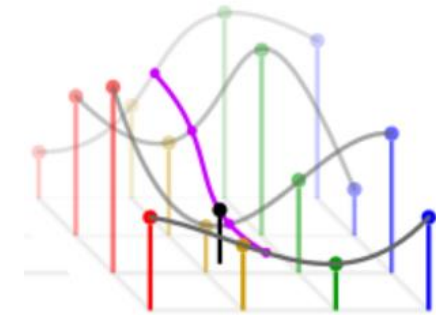


[Image source: Digital Surf]



Extract the grey value profile: the pixels where the searching path pass through within the specified distance

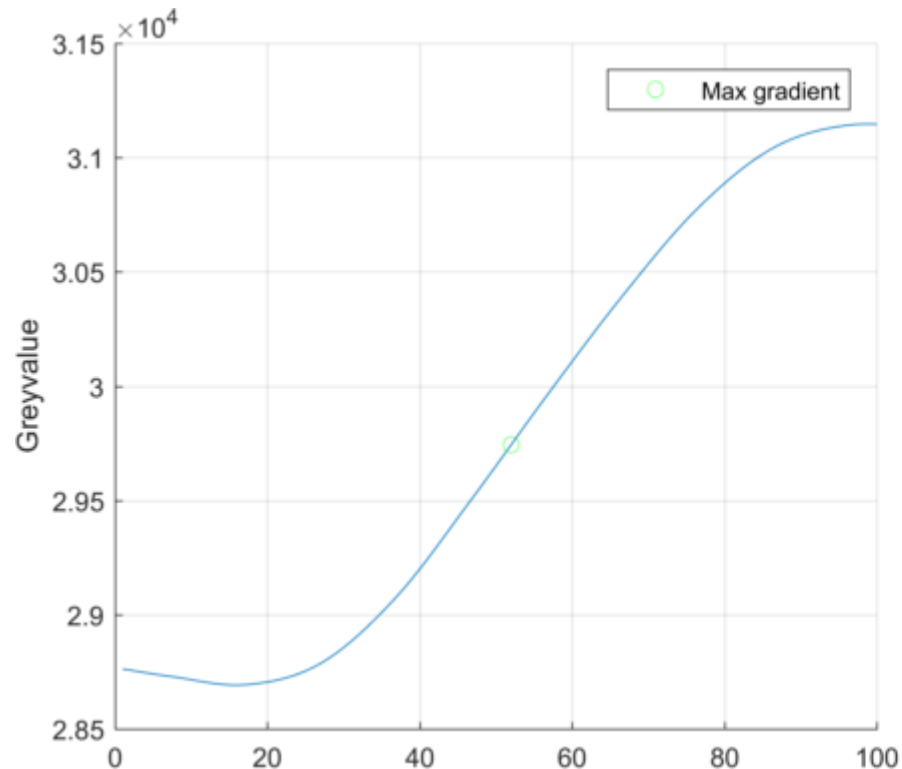
**Bicubic interpolation** is used to locate the maximum gradient position more accurately



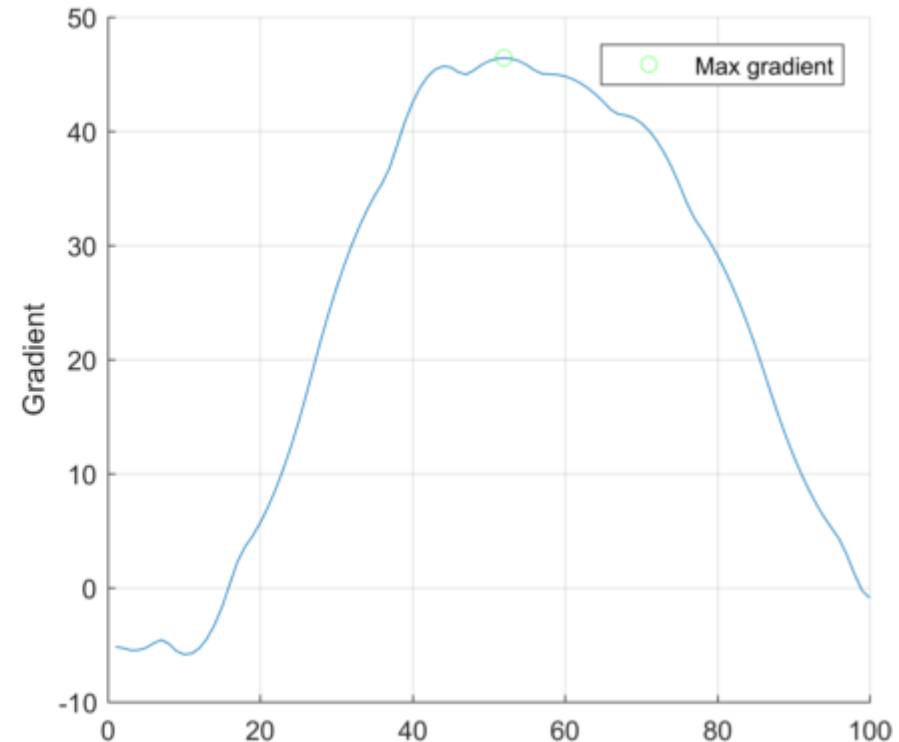
[Image source: Wikipedia]

# 3. 2D Local Searching Algorithms

- Determine the position of maximum gradient: interpolation distance is set to the tenth of pixel size.



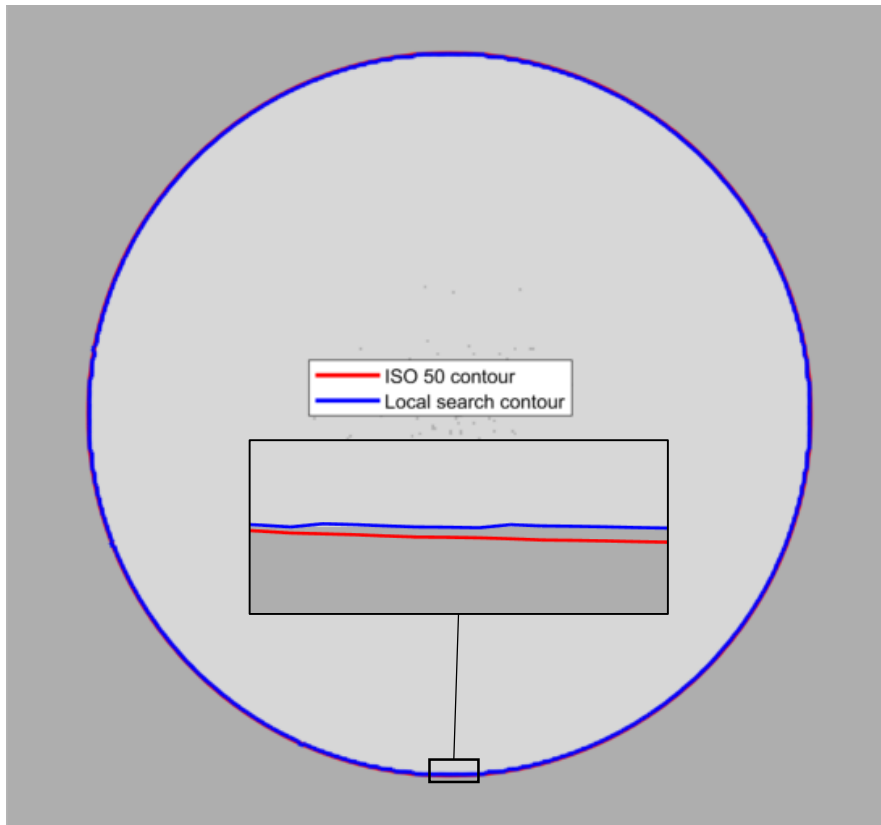
(a) the grey value profile along the search path



(b) the resulted gradient profile

# 4. Initial results

- Smooth cylinder

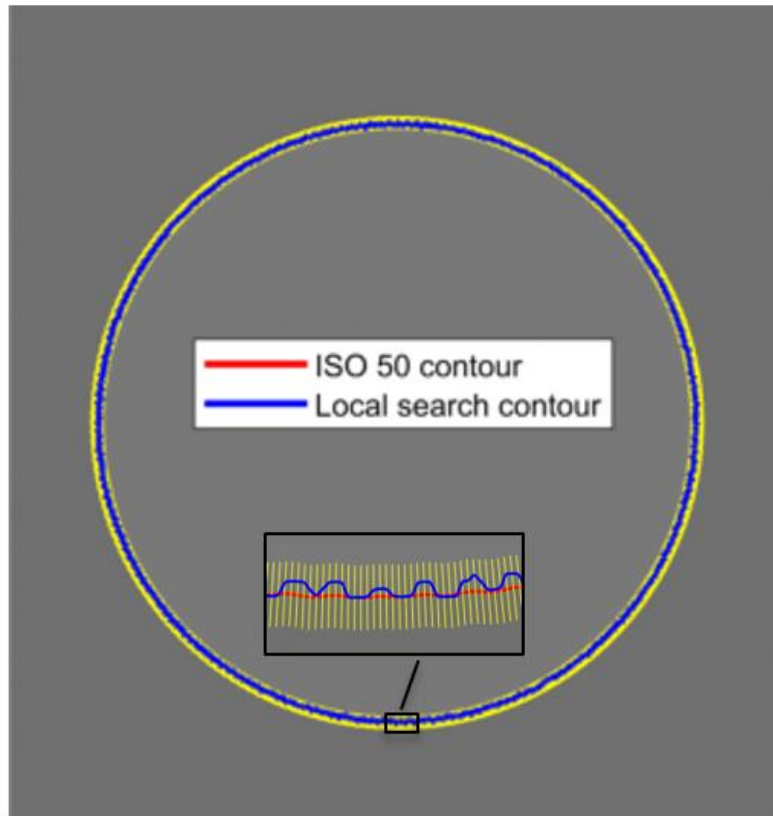


Voxel size (unit: $\mu\text{m}$ )	Cylinder radius (Nominal: 7 mm)			
	ISO 50 (mm)	Deviation ( $\mu\text{m}$ )	Local searching (mm)	Deviation ( $\mu\text{m}$ )
50	7.0229	22.9	7.0087	8.7



# 4. Initial results

- Rough cylinder



Voxel size (unit: $\mu\text{m}$ )	Cylinder radius (Nominal: 7 mm)			
	ISO 50 (mm)	Deviation ( $\mu\text{m}$ )	Local searching (mm)	Deviation ( $\mu\text{m}$ )
40	7.0398	39.8	7.0130	13.0

Voxel size (unit: $\mu\text{m}$ )	Ra (Nominal: 31.8 $\mu\text{m}$ )			
	ISO 50 (mm)	Deviation ( $\mu\text{m}$ )	Local searching (mm)	Deviation ( $\mu\text{m}$ )
40	3.96	-27.84	28.94	-2.86

# 5. Summary and future work

- Summary

- 1) A simulation procedure is proposed to investigate the impact of partial volume effect of XCT to dimensional and surface measurement.
- 2) A 2D local searching algorithm is developed for XCT surface determination.
- 3) Both dimensional and surface texture results show that the local searching algorithm is more accurate than the ISO 50 method.

- Future work

- 1) Subpixel watershed.
- 2) Extend the 2D algorithm to 3D.
- 3) Compare the partial volume effect of XCT to the mechanical filtering effect of CMM measurement for rough surfaces.

# Thank You

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